## Proving Pythagoras' theorem

http://topdrawer.aamt.edu.au/Geometric-reasoning/Good-teaching/Writing-a-proof/Proving-Pythagoras-theorem/Dissected-proof

In any right angled triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides.

Aim: To prove $c^{2}=a^{2}+b^{2}$



| $\frac{c}{b}=\frac{a}{C D}=\frac{b}{y}$ | In $\triangle A B C$ and $\triangle A D C$ |
| :---: | :---: |
| (matching sides of similar triangles) | (both $90^{\circ}$ given) |
| $\angle A C B=\angle A D C$ | $\therefore c^{2}=a^{2}+b^{2}$ |
| $\therefore \triangle A B C \\| \triangle A C D$ | is common |
| $\angle A$ | $\therefore \triangle A B C \\| \triangle C B D$ |
| $\therefore \frac{A B}{A C}=\frac{B C}{C D}=\frac{A C}{A D}$ | $\therefore a^{2}=c x$ |
| (AAA) | $\therefore \quad \frac{c}{b}=\frac{b}{y}$ |
| (both 90 ${ }^{\circ}$ given) | $\therefore b^{2}=c y$ |
| $\angle B$ | (AAA) |
| Now $a^{2}+b^{2}=c x+c y$ | $\angle A C B=\angle B D C$ |
| $=c(c)$ | In $\triangle A B C$ and $\triangle B D C$ |
| (matching sides of similar triangles) | $=c(x+y)$ |
| is common | $=c^{2}$ |
| $\frac{c}{a}=\frac{a}{x}=\frac{b}{C D}$ | $\therefore \frac{A B}{C B}=\frac{B C}{B D}=\frac{A C}{C D}$ |

